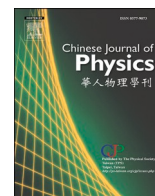




ELSEVIER

Contents lists available at ScienceDirect

## Chinese Journal of Physics

journal homepage: [www.sciencedirect.com/journal/chinese-journal-of-physics](http://www.sciencedirect.com/journal/chinese-journal-of-physics)Size effect on multiferroicity of  $\text{GdMn}_2\text{O}_5$  nanorodsYang-Hsiang Tung<sup>a</sup>, Yi-Jung Chen<sup>a</sup>, Chun-Chuen Yang<sup>a,\*</sup>, Cheng-Yu Weng<sup>a</sup>, Yen-Kai Huang<sup>a</sup>, Yang-Yuan Chen<sup>b</sup>, Maw-Kuen Wu<sup>b</sup><sup>a</sup> Department of Physics, Chung Yuan Christian University, 200, Chung Pei Rd., Chung Li 32023, Taiwan<sup>b</sup> Institute of Physics, Academia Sinica, 128 Sec. 2, Academia Rd., Nankang, Taipei 11529, Taiwan

## A B S T R A C T

Four  $\text{GdMn}_2\text{O}_5$  nanorod samples of various axial lengths ( $\langle L_C \rangle$ ) along the  $c$  axis were synthesized. The antiferromagnetic and ferroelectric ordering disappeared as  $\langle L_C \rangle$  decreased to 66 and 55 nm. Various ferroic critical sizes were observed for the two types of domain sizes. Between  $T = 18$  and 26 K, a charge ordering X-ray diffraction peak appeared at  $\langle L_C \rangle = 79$  nm. This peak was associated with structural distortion and axial length. The broken multiferroicity of the  $\text{GdMn}_2\text{O}_5$  nanorods limits their practical application. For applications in memory devices, the estimated maximal capacity is approximately 650 Gbits/in<sup>2</sup>.

## 1. Introduction

Multiferroics are materials that exhibit two or more ferroic behaviors, including magnetoelectricity, piezoelectricity, and piezomagnetism [1–5]. Multiferroics can be used for fabricating next-generation memory storage devices [5]. Various types of memory devices have been developed using  $\text{BiFeO}_3$ ,  $\text{RMnO}_3$ , and  $\text{RMn}_2\text{O}_5$  compounds, where R stands for rare earth [6–8]. For example, Zavaliche et al. demonstrated an electrically assisted magnetic recording method for the multiferroic nanostructure of  $\text{BiFeO}_3\text{--CoFe}_2\text{O}_4$  [9]. Bibes and Barthélemy designed a novel structure called “MERAM” using magnetoelectric materials for use in memory devices [10]. Yu-Ting Tsai et al. reported high-performance resistance-switching  $\text{Pt/DyMn}_2\text{O}_5/\text{TiN}$  memory devices [8]. These studies indicate the feasibility of designing memory devices using multiferroic materials. Such devices exhibit high stackability and rapid electronic access. However, the physical limitations of multiferroic materials should be clarified. Typical magnets lose their permanent magnetism when their size is smaller than the superparamagnetic limit [11]. This effect is also evident in multiferroics, which places a functional size limit on their applicability. In sandwich structures, the information in each bit is preserved magnetically and accessed electronically [10]. Any improper response of the magnetic or electric signal causes a loss of valuable information. Therefore, the determination of the magnetic and electric critical sizes is crucial for practical applications. Another consideration is driven by the need for the recording density of the multiferroic designs to be comparable with those of current designs. The commercial perpendicular magnetic recording (PMR) technique has improved hard disk recording density by as much as 500–600 Gbits/in<sup>2</sup> and facilitated the fabrication of magnetic recording devices of sizes close to the superparamagnetic limit [12]. In contrast to planar designs, the use of three-dimensional and stackable designs can overcome the size limitation.  $\text{RMn}_2\text{O}_5$  compounds are multiferroic material with magnetoelectric properties [5,13–15]. Due to their electronic configuration and among the rare earth elements, gadolinium exhibits the largest magnetic moment difference between neighboring elements ( $\text{Eu} = 0 \mu_B$ ,  $\text{Gd} = 7.94 \mu_B$ , and  $\text{Tb} = 9.72 \mu_B$ ). This large difference implies that any variation in valence electrons causes large changes in magnetic moment, especially in small-sized samples that have large bounding defects at their surfaces. Furthermore, although magnetic or electric ordering can be induced using

\* Corresponding author.

E-mail address: [chunchuenyang@cycu.edu.tw](mailto:chunchuenyang@cycu.edu.tw) (C.-C. Yang).<https://doi.org/10.1016/j.cjph.2021.01.011>

Received 29 September 2020; Received in revised form 30 December 2020; Accepted 13 January 2021

Available online 4 February 2021

0577-9073/© 2021 The Physical Society of the Republic of China (Taiwan). Published by Elsevier B.V. All rights reserved.

an external field through the magnetoelectric effect, in practice, both orderings must occur spontaneously and simultaneously to preserve information [10]. This study determined the maximum recording density that is set by the critical size associated with the multiferroicity of  $\text{GdMn}_2\text{O}_5$  nanorods. The importance of the size effect in structural, magnetic, and electric properties was also uncovered.

## 2. Sample preparation

$\text{GdMn}_2\text{O}_5$  nanorods were synthesized using a hydrothermal method [16,17]. The obtained powder was divided into five parts and sintered in an electrical furnace at annealing temperatures ( $T_a$ ) of 400, 600, 800, 1000, and 1200 °C. For comparison, a bulk sample was also prepared using the conventional solid-state reaction method.

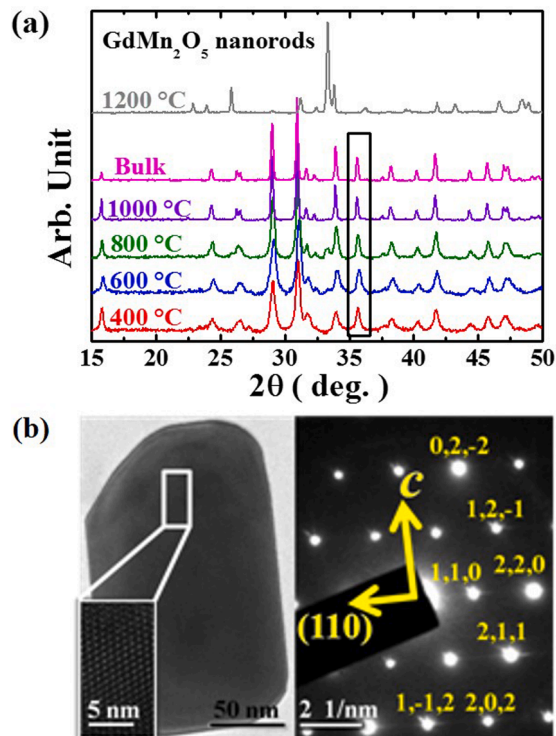
## 3. Experiment

### 3.1. X-ray diffraction

The composition and purity of the sample were determined using a Philips X'pert powder X-ray diffractometer at a  $\text{Cu-K}\alpha$  wavelength. The diffraction patterns were analyzed using the General Structure Analysis System (GSAS) program according to the Rietveld refinement method [18]. Fig. 1(a) presents the obtained patterns, which reveal that the nanorods maintain the same crystal structure as that of the bulk when the annealing temperatures are equal or less than 1000 °C. Structural refinement revealed that the  $\text{GdMn}_2\text{O}_5$  nanorods and bulk samples exhibited orthorhombic  $Pb_{21}m$  symmetry [19,20]. As  $T_a$  increased to 1200 °C,  $\text{GdMn}_2\text{O}_5$  decomposed into two major compounds, namely  $\text{GdMnO}_3$  and  $\text{Mn}_3\text{O}_4$ , at a molar ratio of approximately 71% to 29% [19]. The size of the nanorods was correlated with the annealing temperature. The full width half maximum (FWHM) of the  $\{112\}$  single peak at  $2\theta = 35.6^\circ$  decreased with increasing of  $T_a$ , which indicated that the size of the samples increased with annealing temperature.

### 3.2. Transmission electron microscopy images

To quantify the sizes of the four types of single-phase  $\text{GdMn}_2\text{O}_5$  nanorods, JEOL JEM-2100 field emission transmission electron microscopy (FE-TEM) and selection area electron diffraction (SAED) were performed to determine the axial/radial lengths and their directions [21]. Fig. 1(b) displays the results of the  $T_a = 1000^\circ\text{C}$  sample. The FE-TEM images and SAED patterns reveal that the  $c$  axis



**Fig. 1.** (a) X-ray diffraction patterns of  $\text{GdMn}_2\text{O}_5$  bulk and nanorods at various annealing temperatures ( $T_a$ ) of 400, 600, 800, 1000, and 1200 °C. (b) Transmission electron microscopy (TEM) image of ( $L_c$ ) = 198 nm  $\text{GdMn}_2\text{O}_5$  nanorods. Inset image displays the selected area electron diffraction (SAED) patterns and high-resolution electron microscopic images.

of the crystal is parallel to the axial direction of the nanorods [16]. This phenomenon was also observed in nanorods annealed at  $T_a = 400, 600, 800,$  and  $1000\text{ }^\circ\text{C}$ . A similar phenomenon was not observed for the radial direction with a specified orientation. By contrast, the mean measured values of the axial length (error bar)  $\times$  radial length (error bar) for the samples with  $T_a = 400, 600, 800,$  and  $1000\text{ }^\circ\text{C}$  were  $55(10)\text{ nm} \times 26(7)\text{ nm}, 66(10)\text{ nm} \times 31(6)\text{ nm}, 79(12)\text{ nm} \times 31(5)\text{ nm},$  and  $198(43)\text{ nm} \times 99(26)\text{ nm},$  respectively. For brevity and to provide crystal orientation, the samples are referred to by their mean axial lengths,  $\langle L_C \rangle,$  rather than their  $T_a$ .

### 3.3. Magnetic properties

AC magnetic susceptibility measurements were performed using a quantum-design physical property measurement system (PPMS) from Quantum Design with the standard setup. The sample was subjected to a weak driving AC magnetic field at 10 Oe with a frequency of  $10^3\text{ Hz}$  ( $f_m$ ). Fig. 2(a) displays the collected temperature profiles of the in-phase component  $\chi'$  of the bulk, at  $\langle L_C \rangle = 198, 79, 66,$  and  $55\text{ nm}$ . The  $\chi'$ - $T$  curve of the bulk reveals a magnetic susceptibility increase at  $43\text{ K}$  ( $T^*$ ). This increase is associated with the starting of the incommensurate antiferromagnetic ordering of Mn ions [20]. Simultaneously, a small distinct feature that is related to the transition from incommensurate to commensurate antiferromagnetic ordering was observed at  $41.5\text{ K}$  ( $T_{CAF}$ ) [20]. For samples with  $\langle L_C \rangle = 198$  and  $79\text{ nm}$ , the values of  $T^*$  and  $T_{CAF}$  were 2 and 1 K lower, respectively, than those of the bulk. By contrast, no antiferromagnetic (AFM) peaks were observed when  $\langle L_C \rangle$  was 66 and 55 nm. When above 80 K, all samples were in the paramagnetic phase. The effective magnetic moment ( $\mu_{eff}$ ) and Néel temperature ( $T_N$ ) in Fig. 2(b) were obtained by curve fitting using the Curie–Weiss law. Both  $\mu_{eff}$  and  $T_N$  reduced with decreasing  $\langle L_C \rangle$ . An abrupt decrease in both parameters occurred between  $\langle L_C \rangle = 79$  and 66 nm, which corresponded with the disappearance of the AFM peak in Fig. 2(a). As  $\langle L_C \rangle$  decreased, both  $T^*$  and  $T_N$  shifted to lower temperatures, which implied that the size effect weakened the magnetic coupling between Mn ions. Both figures reveal that the critical length of magnetic ordering was between 66 and 79 nm. Notably, the radial lengths of  $\langle L_C \rangle = 55, 66,$  and  $79\text{ nm}$  were all near 30 nm to within the statistical error, which indicated that the critical length of AFM magnetic ordering may not be obviously correlated with the radial length but governed by the correlation length along the  $c$  axis of the crystal ( $\langle L_C \rangle$  length).

### 3.4. Dielectric properties

The effects of the size on the dielectric properties of the nanorods were investigated. Samples were packed, wired, and placed in a closed-cycle refrigerator with precise temperature maintenance using a Lakeshore 325 temperature controller. An Agilent E4980A LCR meter was used to measure the capacitance of the samples in excited AC electric fields of various frequencies ( $f_e$ ). The in-phase relative dielectric constant  $\epsilon'$  was calculated from the measured capacitance. Here, the porosity ( $P$ ) of each sample was between 33% and 35%, which is the contribution of the vacuum. Fig. 3(a) illustrates the  $\epsilon'$  of the bulk for the samples with  $\langle L_C \rangle = 79, 66,$  and  $55\text{ nm}$  at  $f_e = 10^3$

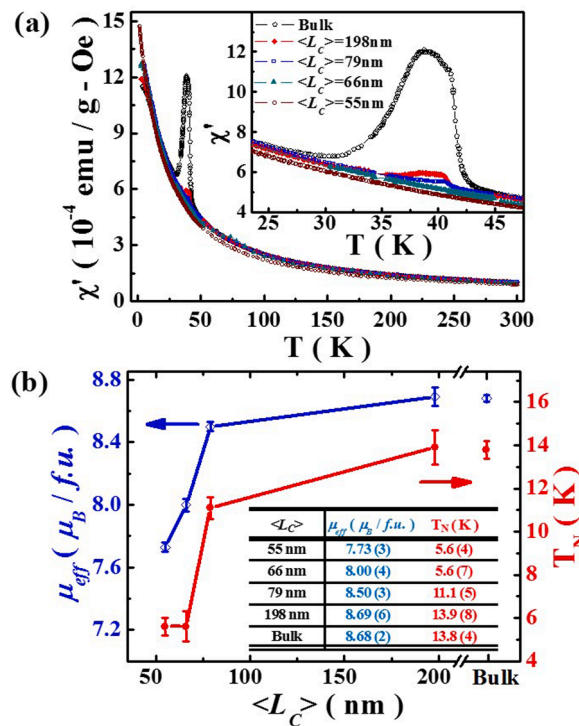


Fig. 2. (a)  $\chi'$ - $T$  curves of bulk,  $\langle L_C \rangle = 198, 79, 66,$  and  $55\text{ nm}$  nanorods. (b) Fitted effective magnetic moment  $\mu_{eff}$  and Néel temperature  $T_N$  of four nanorod and one bulk samples.

Hz. The corresponding ferroelectric (FE) ordering temperatures ( $T_c$ ) were approximately 38, 42, 43 K, and unavailable, respectively. Here,  $T_c$  increased as the size became larger than 55 nm. Moreover, the saturated dielectric constant ( $\epsilon_s'$ ) of FE ordering at approximately 14 K decreased as the size decreased. The critical size of FE ordering was 55 nm, which is smaller than the 66 nm of AFM. This observation implies that the FE domain is smaller than that of AFM and can hold finite FE ordering at 66 nm. Otherwise, the FE domain is sensitive to the frequency of the AC electric field. Fig. 3(b), (c), and (d) display the results of  $\langle L_c \rangle = 79, 66,$  and  $55$  nm samples at frequencies from  $10^3$  to  $10^6$  Hz. The  $\epsilon_s'$  of all three samples decreased with increasing frequency. Compared with the reduction of  $\epsilon'$  (i. e.,  $\Delta\epsilon'$ ) at  $f_e = 10^6$  Hz between the samples with the  $\langle L_c \rangle$  of 79 and 66 nm, the  $\Delta\epsilon'$  value between 14 ( $\epsilon_s'$ ) and 45 K (above  $T_c$ ) of the sample with  $\langle L_c \rangle = 79$  nm was finite. By contrast, the  $\Delta\epsilon'$  of the sample with  $\langle L_c \rangle = 66$  nm was almost zero. This finding implies a correlation between frequency and axial length in the nanorods.

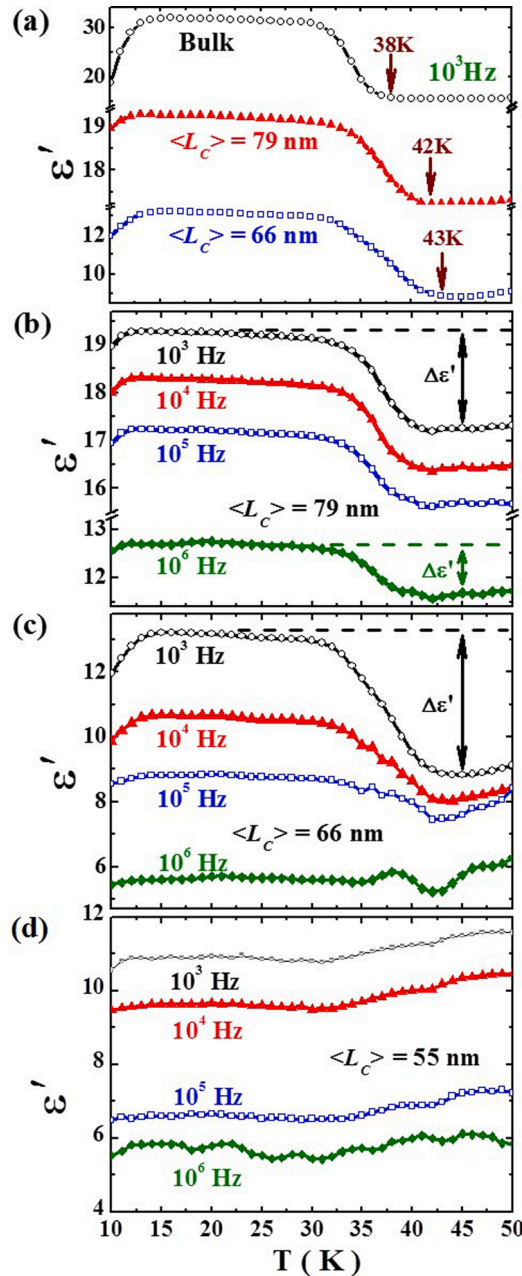


Fig. 3. (a) Measured relative dielectric constants of bulk for  $\langle L_c \rangle = 79, 66,$  and  $55$  nm samples excited at an AC frequency of  $10^3$  Hz. Samples with  $\langle L_c \rangle =$  (b) 79 nm, (c) 66 nm, and (d) 55 nm at various AC frequencies.

4. Discussion

Several studies have reported that the polarization of the AFM domain in the multiferroic materials is governed by FE polarizations, which originate from the coupling between FE and AFM domain walls (DWs) and result in excellent tunability by the external electric field [22–24]. By contrast, some AFM domains located at structural defects do not easily change their polarization and result in frozen coupled FE DWs. This behavior results in bad response at higher frequencies. Furthermore, the structural defects typically occur at sample surfaces (which have abnormal bonds), and these defects are especially critical in nanorods with a large surface-to-volume ratio. Therefore, materials with smaller  $\langle L_C \rangle$  exhibit lower  $\epsilon'$  than materials with larger  $\langle L_C \rangle$  do (Fig. 3[a]). The difference between the values of  $\mu_{eff}$  for the nanorods and the bulk can be used to estimate the portion of AFM DWs located at structural defects. Magnetic moments that are at the surface may not respond to an excited AC magnetic field and may have a lower contribution to  $\mu_{eff}$ . The reduction of  $\mu_{eff}$  of the bulk by this effect can be neglected so that the  $\mu_{eff}$  of the bulk ( $\mu_{eff}^{bulk}$ ) to be used as a standard for comparison. Here, the ratio of the surface defects of  $\langle L_C \rangle = 66$  to  $79$  nm was estimated to be  $(\mu_{eff}^{bulk} - \mu_{eff}^{66\text{ nm}}) / (\mu_{eff}^{bulk} - \mu_{eff}^{79\text{ nm}}) = 0.68 \pm 0.06 / 0.18 \pm 0.05 = 3.8 \pm 1.9$  (from the table in Fig. 2(b)), which is close to the reduction ratio of  $(\Delta\epsilon'_{1\text{KHz}}^{66\text{ nm}} - \Delta\epsilon'_{1\text{MHz}}^{66\text{ nm}}) / (\Delta\epsilon'_{1\text{KHz}}^{79\text{ nm}} - \Delta\epsilon'_{1\text{MHz}}^{79\text{ nm}}) = 4.3/1 = 4.3$  (from Fig. 3(b) and (c)). These calculations verified the previous inference and reveal the consistency between magnetic and electric properties.

The mechanism of magnetoelectric coupling involves simultaneous magnetic and electric ordering and is governed by structural distortions [20]. These distortions can be attributed to the size effect. To investigate the relationship between structural distortions and the size effect, in situ X-ray diffraction (XRD) was performed on  $\langle L_C \rangle = 66$  and  $79$  nm samples, whose lengths were close to the critical limits, at various temperatures from 10 to 55 K at intervals of 5 K [25]. Fig. 4(a) displays the results of the refinement of  $\langle L_C \rangle = 79$  nm at 25 K. An additional peak was observed at  $2\theta = 27.3^\circ$ . This peak was not indexed by the orthorhombic  $Pbam$  symmetry. Many space groups, including  $Pb2_1m$  symmetry, have been tested in the refinement, but no group has matched the peak [20,26]. The  $\langle L_C \rangle = 66$  nm sample did not exhibit this peak in the temperatures of interest. To trace the evolution of the peak, experiments were conducted again between 15 and 30 K at 1 K intervals with  $2\theta = 25^\circ - 30^\circ$ . Fig. 4(b) displays the temperature profile of the  $\langle L_C \rangle = 79$  nm sample, which

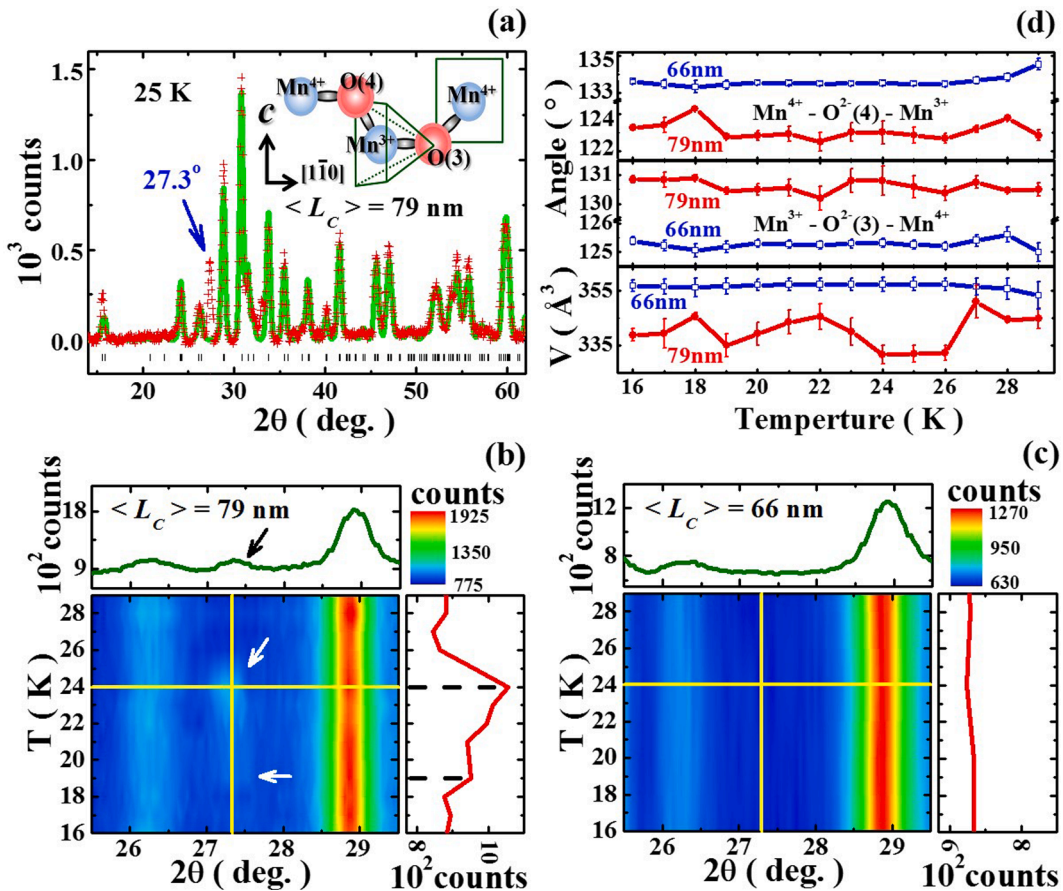


Fig. 4. (a) Refinement results from X-ray diffraction pattern for  $\langle L_C \rangle = 79$  nm at 25 K. Observed (red crosses) and calculated (green solid line) values with estimated peak positions (black dash) are presented. Diffraction patterns obtained at various temperatures for (b)  $\langle L_C \rangle = 79$  nm and (c)  $\langle L_C \rangle = 66$  nm nanorods are also plotted. (d) Refined cell volume and  $\text{Mn}^{3+}\text{-O}^{2-}\text{-Mn}^{4+}$  angles of  $\langle L_C \rangle = 79$  nm and  $\langle L_C \rangle = 66$  nm.



exhibited an additional peak at approximately 18 K and suddenly disappeared at 27 K. Two local maxima were observed at 19 and 24 K. No similar observations were made for the  $\langle L_C \rangle = 66$  nm sample in Fig. 4(c). Fig. 4(d) displays the cell volume and the  $\text{Mn}^{3+}$ -O- $\text{Mn}^{4+}$  bond angles of both samples. The variation of the  $\langle L_C \rangle = 79$  nm sample was larger than that of the  $\langle L_C \rangle = 66$  nm sample. In Fig. 4(b), two local cell volume minima are illustrated to be associated with two local maxima of the additional peak. Moreover, the  $\text{Mn}^{4+}$ - $\text{O}^{2-}$ (4)- $\text{Mn}^{3+}$ - $\text{O}^{2-}$ (3)- $\text{Mn}^{4+}$  chain is roughly extended in the  $[1\bar{1}0]$  direction and confined by the radial length. The inset in Fig. 4(a) displays the Mn and O positions at the pyramid and the plane through the middle of an octahedron. The radial lengths of the two samples were almost equal, which implied that the only differences between the two samples were the mean axial length. This study revealed that increasing the axial length reduced the cell volume and created distortions inside the unit cell, which resulted in periodic charge ordering. The charge ordering peak at  $27.3^\circ$  can be indexed as  $\{2\ 1\ \frac{1}{2}\}$ , and its intensity varies with the extent of distortion. Giovannetti et al. reported theoretical calculations concerning similar phenomena that involved the transfer of charges between manganese and oxygen ions and proposed a relationship between distortion and bond lengths [26].

## 5. Conclusion

The magnetic, electric, and structural properties of nanorods with various  $\langle L_C \rangle$  were investigated. Multiferroicity is broken by the disappearance of AFM ordering when  $\langle L_C \rangle$  is 66 nm. The FE ordering was suppressed when  $\langle L_C \rangle$  is 55 nm. Smaller  $\langle L_C \rangle$  result in larger surface defects to volume ratio and hinder the motion of FE DWs. Therefore,  $\epsilon'$  decreases as size decreases and results in a bad response to high frequencies. XRD experiments on the  $\langle L_C \rangle = 79$  nm sample between 18 and 26 K yielded a charge ordering peak at  $27.3^\circ$ , which was indexed as  $\{2\ 1\ \frac{1}{2}\}$ , and its appearance was correlated with the  $\langle L_C \rangle$  length. The magnetic, electric, and structural properties were governed by the axial lengths of nanorods. In practice, the memory capacity of  $\text{GdMn}_2\text{O}_5$  nanorods can be calculated by minimizing their functional size by fabricating upstanding pillars with a cross-sectional area of  $31\ \text{nm}^2$ . Therefore, the estimated maximal capacity was approximately 650 Gbits/in<sup>2</sup>.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Acknowledgements

This work is supported by the Ministry of Science and Technology of Taiwan, under grant no. MOST 108–2112-M-033–005 and MOST 109–2112-M-033–008.

## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at [doi:10.1016/j.cjph.2021.01.011](https://doi.org/10.1016/j.cjph.2021.01.011).

## Reference

- [1] E. Ascher, H. Rieder, H. Schmid, H. Stössel, Some properties of ferromagnetoelectric Nickel-Iodine boracite,  $\text{Ni}_3\text{B}_7\text{O}_{13}\text{I}$ , *J. Appl. Phys.* 37 (1966) 1404.
- [2] Hans Schmid, Multi-ferroic magnetoelectrics, *Ferroelectrics* 162 (1994) 317.
- [3] Nicola A. Spaldin, Manfred Fiebig, The renaissance of magnetoelectric multiferroics, *Science* 309 (2005) 391.
- [4] W. Eerenstein, N.D. Mathur, J.F. Scott, Multiferroic and magnetoelectric materials, *Nature* 442 (2006) 759.
- [5] Nicola A. Spaldin, Sang-Wook Cheong, Ramamoorthy. Ramesh, Multiferroics: past, present, and future, *Phys Today* 63 (2010) 38.
- [6] S.Y. Yang, F. Zavaliche, L. Mohaddes-Ardabili, V. Vaithyanathan, D.G. Schlom, Y.J. Lee, Y.H. Chu, M.P. Cruz, Q. Zhan, T. Zhao, R. Ramesh, Metalorganic chemical vapor deposition of lead-free ferroelectric  $\text{BiFeO}_3$  films for memory applications, *Appl. Phys. Lett.* 87 (2005), 102903.
- [7] H.T. Yi, T. Choi, S.-W. Cheong, Reversible colossal resistance switching in  $(\text{La,Pr,Ca})\text{MnO}_3$ : cryogenic nonvolatile memories, *Appl. Phys. Lett.* 95 (2009), 063509.
- [8] Yu-Ting Tsai, Ting-Chang Chang, Wei-Li Huang, Chih-Wen Huang, Yong-En Syu, Shih-Cheng Chen, Simon M. Sze, Ming-Jinn Tsai, Tseung-Yuen Tseng, Investigation for coexistence of dual resistive switching characteristics in  $\text{DyMn}_2\text{O}_5$  memory devices, *Appl. Phys. Lett.* 99 (2011), 092106.
- [9] F. Zavaliche, T. Zhao, H. Zheng, F. Straub, M.P. Cruz, P.-L. Yang, D. Hao, R. Ramesh, Electrically assisted magnetic recording in multiferroic nanostructures, *Nano Lett* 7 (2007) 1586.
- [10] Manuel Bibes, Agnès Barthélémy, Towards a magnetoelectric memory, *Nat Mater* 7 (2008) 425.
- [11] Charles Kittel, Theory of the Structure of ferromagnetic domains in films and small particles, *Phys. Rev.* 70 (1946) 965.
- [12] S.N. Piramanayagam, Perpendicular recording media for hard disk drives, *J. Appl. Phys.* 102 (2007), 011301.
- [13] N. Hur, S. Park, P.A. Sharma, J.S. Ahn, S. Guha, S.-W. Cheong, Electric polarization reversal and memory in a multiferroic material induced by magnetic fields, *Nature* 429 (2004) 392.
- [14] Hiroyuki Tsujino, Kay Kohn, Magnetoelectric effect of  $\text{GdMn}_2\text{O}_5$  single crystal, *Solid State Commun* 83 (1992) 639.
- [15] B.M. Kadamtseva, S.S. Krotov, Yu.F. Popov, G.P. Vorob'ev, Features of the magnetoelectric behavior of the family of multiferroics  $\text{RMn}_2\text{O}_5$  at high magnetic fields, *Low Temp. Phys.* 32 (2006) 709.
- [16] Jian-Tao Han, Yun-Hui Huang, Wei Huang, John B. Goodenough, Selective synthesis of  $\text{TbMn}_2\text{O}_5$  nanorods and  $\text{TbMnO}_3$  micron crystals, *J. Am. Chem. Soc.* 128 (2006) 14454.
- [17] Gangqiang Zhu, Peng Liu, Mirabbos Hojamberdiev, Bao Ge, Yun Liu, Hongyan Miao, Guoqiang Tan, Synthesis  $\text{RMn}_2\text{O}_5$  (R = Gd and Sm) nano- and microstructures by a simple hydrothermal method, *Mater Chem Phys* 118 (2009) 467.

- [18] A.C. Larson, R.B. Von Dreele, General Structure Analysis System (GSAS), Los Alamos National Laboratory Report LAUR, 1994, pp. 86–748.
- [19] See supplementary material Fig. S1.
- [20] L.C. Chapon, G.R. Blake, M.J. Gutmann, S. Park, N. Hur, P.G. Radaelli, S.-W. Cheong, Structural anomalies and multiferroic behavior in magnetically frustrated  $\text{TbMn}_2\text{O}_5$ , *Phys. Rev. Lett.* 93 (2004), 177402.
- [21] See supplementary material Fig. S2.
- [22] V. Skumryev, V. Laukhin, I. Fina, X. Martí, F. Sánchez, M. Gospodinov, J. Fontcuberta, Magnetization reversal by electric-field decoupling of magnetic and ferroelectric domain walls in multiferroic-based heterostructures, *Phys. Rev. Lett.* 106 (2011), 057206.
- [23] M. Fiebig, Th. Lottermoser, D. Fröhlich, A.V. Goltsev, R.V. Pisarev, Observation of coupled magnetic and electric domains, *Nature* 419 (2002) 818.
- [24] F. Kagawa, M. Mochizuki, Y. Onose, H. Murakawa, Y. Kaneko, N. Furukawa, Y. Tokura, Dynamics of multiferroic domain wall in spin-cycloidal ferroelectric  $\text{DyMnO}_3$ , *Phys. Rev. Lett.* 102 (2009), 057604.
- [25] See supplementary material Fig. S3.
- [26] Gianluca Giovannetti, Jeroen van den Brink, Electronic correlations decimate the ferroelectric polarization of multiferroic  $\text{HoMn}_2\text{O}_5$ , *Phys. Rev. Lett.* 100 (2008), 227603.